Analysis of Algorithms

Problem 5-1

Solve the following recurrence: $na_n = (n+1)a_{n-1} + 2n$ for $n \ge 1$ and $a_0 = 0$.

Problem 5-2

Compute the number of iterations of the while-loop for 0 < i and arbitrary j.

```
while ( i <= j ) {
    i = i + j;
    if ( i > j ) then j = j + 10;
}
```

Problem 5-2

Given an array a of length n, an algorithm compares all pairs (a[i], a[j]) for all $i < j \le n$, and then calls itself recursively on all proper prefixes of a.

How often does the algorithm compare two pairs? Use the repertoire method!

Homework Assignment 5-1 (10 Points)

Use summation factors to solve the following recurrence:

$$a_0 = 0$$

 $a_n = \frac{a_{n-1}}{n} + \frac{1}{(n-1)!}$ for $n \ge 1$

Homework Assignment 5-2 (10 Points)

Use the repertoire method to find a closed form for the following recurrence:

$$\begin{aligned} a_0 &= 5\\ a_1 &= 9\\ a_n &= na_{n-1} + n^2 a_{n-2} - n^4 - 3n^2 + 5 \qquad \text{for } n \ge 2 \end{aligned}$$